

Name KEY

Solve each system of equations using the *substitution* method. Show your work!

1) $x = 6 + y$
 $2x + y = 0$

$$\begin{aligned} 2(6+y) + y &= 0 \\ 12 + 2y + y &= 0 \\ 12 + 3y &= 0 \\ 3y &= -12 \\ y &= -4 \end{aligned}$$

$$\begin{aligned} x &= 6 + y \\ x &= 6 + (-4) \\ x &= 2 \end{aligned}$$

$(2, -4)$

2) $3x + 5y = 15$
 $x - y = 4 \rightarrow x = y + 4$

$$\begin{aligned} 3(y+4) + 5y &= 15 \\ 3y + 12 + 5y &= 15 \\ 8y + 12 &= 15 \\ 8y &= 3 \\ y &= \frac{3}{8} \end{aligned}$$

$$\begin{aligned} x &= y + 4 \\ x &= \frac{3}{8} + 4 \end{aligned}$$

$x = 4\frac{3}{8} \quad (4\frac{3}{8}, \frac{3}{8})$

3) $6x - 3y = 9$
 $\frac{y+3}{2} = x$

$$\begin{aligned} 3\left(\frac{y+3}{2}\right) - 3y &= 9 \\ 3y + 9 - 3y &= 9 \\ 9 &= 9 \end{aligned}$$

true statement

Infinitely many solutions

Solve each system of equations using the *elimination* method. Show your work!

4) $7y - 2x = 10$
 $2y + 2x = -1$

$$\begin{aligned} 9y &= 9 \\ y &= 1 \end{aligned}$$

$$\begin{aligned} 2y + 2x &= -1 \\ 2(1) + 2x &= -1 \end{aligned}$$

$$\begin{aligned} 2x &= -3 \\ x &= -\frac{3}{2} \end{aligned}$$

$(-\frac{3}{2}, 1)$

5) $2(2x - y = -1)$
 $3x + 2y = 30$

$$\begin{aligned} 4x - 2y &= -2 \\ 3x + 2y &= 30 \end{aligned}$$

$$\begin{aligned} 7x &= 28 \\ x &= 4 \end{aligned}$$

$$\begin{aligned} 3x + 2y &= 30 \\ 3(4) + 2y &= 30 \\ 12 + 2y &= 30 \\ 2y &= 18 \\ y &= 9 \end{aligned}$$

$(4, 9)$

6) $-2(3x + 5y = 10)$
 $3(2x - 3y = 4)$

$$\begin{aligned} -6x - 10y &= -20 \\ 6x - 9y &= 12 \\ -19y &= -8 \\ y &= 8/19 \end{aligned}$$

Start over, cancel y

$$\begin{aligned} 9x + 15y &= 30 \\ 10x - 15y &= 20 \end{aligned}$$

$$\begin{aligned} 19x &= 50 \\ x &= 50/19 \quad (\frac{50}{19}, \frac{8}{19}) \end{aligned}$$

For each system, fill in the blanks with the number(s) you would need to multiply each equation by to *eliminate* (cancel) "y". If an equation should not change, write "no change".

7) no chg $2x - 8y = 1$
4 $5x + 2y = -1$

8) -3 $x + \frac{1}{3}y = 9$
no chg $3x + y = 7$

9) 2 $x - 6y = 0$
-3 $6x - 4y = 3$

↑ Answers may vary ↑

Solve each system of equations using the **graphing** method. Show your graphs, but write the solution in the blank! Solve for y on this page if necessary. **Graphs on next page.**

$$\begin{aligned}
 10) \quad & x + 1 = y \\
 & 2x - 2y = 8 \\
 & -2y = -2x + 8 \\
 & y = x - 4
 \end{aligned}$$

Solution: ∅

$$\begin{aligned}
 11) \quad & 2x + 3y = 12 \\
 & y = 2x - 4 \\
 & 3y = -2x + 12 \\
 & y = -\frac{2}{3}x + 4
 \end{aligned}$$

Solution: (3, 2)

$$\begin{aligned}
 12) \quad & x + y = 6 \rightarrow y = -x + 6 \\
 & 3x - 4y = 4 \\
 & -4y = -3x + 4 \\
 & y = \frac{3}{4}x - 1
 \end{aligned}$$

Solution: (4, 2)

Solve each **system of inequalities**. Shade the proper area on the graph to show the solutions. Solve for y on this page if necessary. **Graphs on next page**

$$\begin{aligned}
 13) \quad & y + 2 \leq 7 \\
 & y + 4 \geq -3x
 \end{aligned}$$

$$\begin{aligned}
 14) \quad & y > |x| - 2 \\
 & y < |x + 1| + 4
 \end{aligned}$$

$$\begin{aligned}
 15) \quad & y \leq -2|x| \\
 & x < 1 \\
 & 3y + 3x \geq -9
 \end{aligned}$$

Solve each of these systems with whatever method you feel is best.

$$\begin{aligned}
 16) \quad & -2(8x + 3y + 5 = 0) \\
 & 10x + 6y + 13 = 0 \quad \left(\frac{1}{2}, -3\right)
 \end{aligned}$$

$$\begin{aligned}
 17) \quad & y = 2x - 3 \\
 & y = -\frac{1}{2}x + 2 \quad (2, 1)
 \end{aligned}$$

$$\begin{aligned}
 -16x - 6y - 10 &= 0 \\
 10x + 6y + 13 &= 0 \\
 \hline
 \end{aligned}$$

$$\begin{aligned}
 -6x + 3 &= 0 \\
 -6x &= -3 \\
 x &= \frac{1}{2}
 \end{aligned}$$

$$\begin{aligned}
 8x + 3y + 5 &= 0 \\
 8\left(\frac{1}{2}\right) + 3y + 5 &= 0 \\
 4 + 3y + 5 &= 0 \\
 3y + 9 &= 0 \\
 3y &= -9 \\
 y &= -3
 \end{aligned}$$

$$18) \quad \frac{x}{4} - \frac{y}{3} = 1 \quad \text{and} \quad \frac{1}{3}x - \frac{4}{9}y = \frac{4}{3}$$

Get common denominators first.

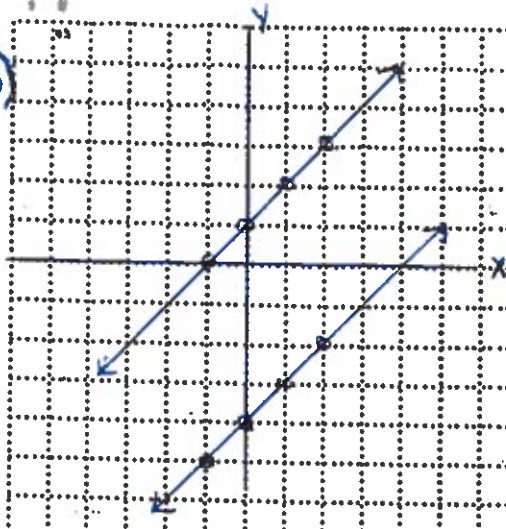
$$\frac{3x}{12} - \frac{4y}{12} = \frac{12}{12} \quad \frac{3}{9}x - \frac{4}{9}y = \frac{12}{9}$$

$$3x - 4y = 12 \quad 3x - 4y = 12$$

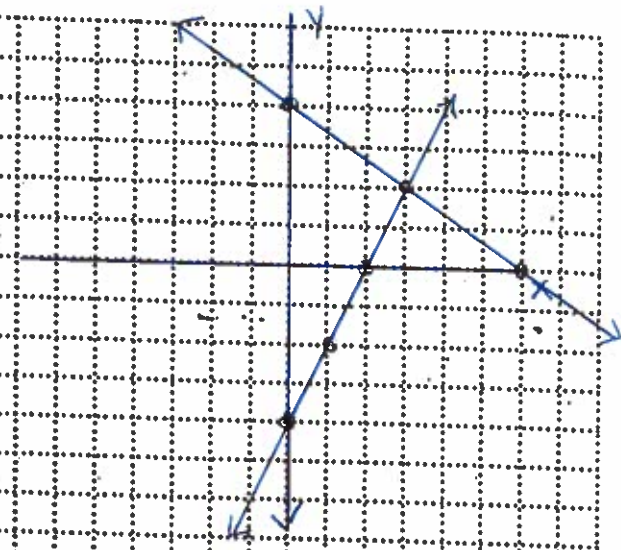
Same equation: Infinitely many solutions

Graph is on next page

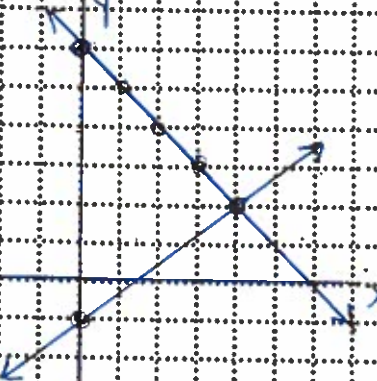
10)



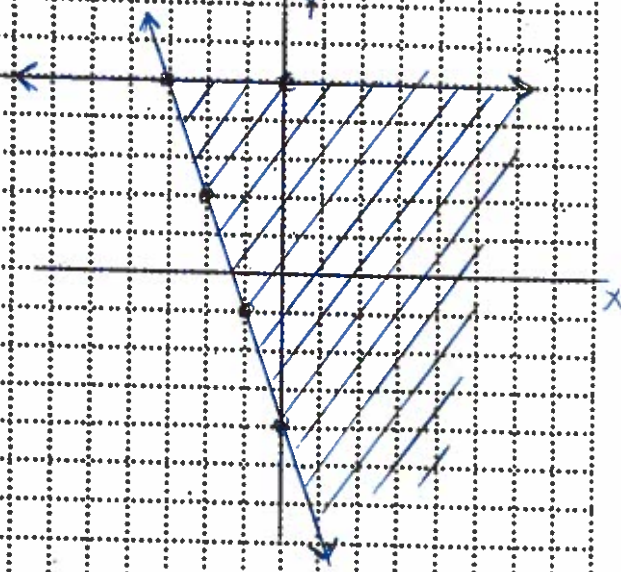
11)



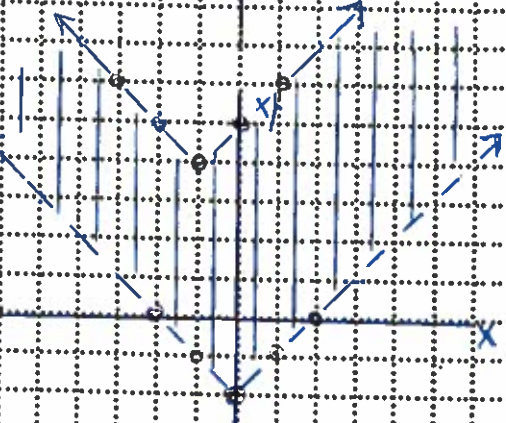
12)



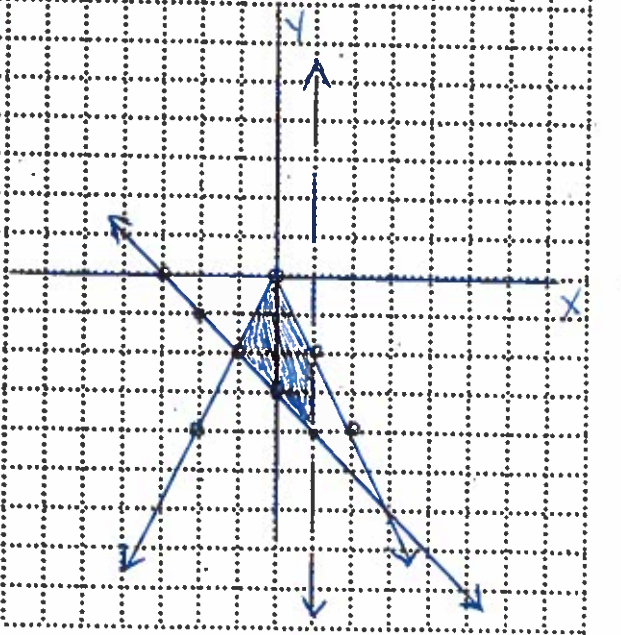
13)



14)



15)



17)

