

Note page for Simplifying Radicals

Simplifying examples: Treat them like factor trees (literally)

1) without negative

2) with negative

$$\begin{aligned} &\sqrt{48x^2} \\ &\sqrt{6}\sqrt{8}\sqrt{x}\sqrt{x} \\ &\sqrt{2}\sqrt{3}\sqrt{2}\sqrt{4}\sqrt{x}\sqrt{x} \\ &\textcircled{\sqrt{2}}\sqrt{3}\textcircled{\sqrt{2}}\textcircled{\sqrt{2}}\textcircled{\sqrt{2}}\textcircled{x}\textcircled{x} \end{aligned}$$

$$\begin{aligned} &\sqrt{-50} \\ &\sqrt{-1}\sqrt{50} \\ &\sqrt{-1}\sqrt{2}\sqrt{25} \\ &\sqrt{-1}\sqrt{2}\textcircled{\sqrt{5}\sqrt{5}} \end{aligned}$$

Circle any pairs you see and use one of those numbers as your outside total. The square root of $-1 = i$

Answer: $2 \cdot 2x\sqrt{3}$
 $= 4x\sqrt{3}$

$= 5i\sqrt{2}$

Multiply and divide examples: Treat mult. problems like the above.

1) $(7\sqrt{10})(3\sqrt{-14})$

$7\textcircled{\sqrt{2}}\sqrt{5} \cdot 3\sqrt{-1}\textcircled{\sqrt{2}}\sqrt{7}$

$7 \cdot 3 \cdot 2 \cdot i \sqrt{5}\sqrt{7}$

$= 42i\sqrt{35}$

2) $\frac{\sqrt{120}}{\sqrt{30}}$

combine as one

$\sqrt{\frac{120}{30}}$

$\sqrt{4}$

$= 2$

3) $\sqrt{\frac{3}{100}}$

split into two

$\frac{\sqrt{3}}{\sqrt{100}}$

since $\sqrt{100} = 10$

$= \frac{\sqrt{3}}{10}$ done!

Examples using imaginary numbers (i)

Treat the "i" like any other variable, then consult the i-chart to simplify

i-chart	
$\sqrt{-1} = i$	$i^2 = -1$
$i^3 = -i$	$i^4 = 1$

1) $-5i^2 \cdot 4i$
 $-20i^3$
 $-20 \cdot -i$
 $= 20i$

2) $(3i)^3(2i^4)$
 $(27i^3)(2i^4)$
 $(27 \cdot -i)(2 \cdot 1)$
 $54 \cdot -i$
 $= -54i$

3) i^{39}
 $i^{36} \cdot i^3$ (find a multiple of 4)
 $(i^4)^9 \cdot i^3$
 $(1)^9 \cdot i^3$
 $1 \cdot -i$
 $= -i$