

COMPLETING THE SQUARE

The SQUARE ROOT Property

Factor perfect square problems, then take the **square root!**

Example: $x^2 - 14x + 49 = 144$
 when in doubt, factor it out!
 $(x - 7)(x - 7) = 144$
 $(x - 7)^2 = 144$
 square root both sides
 $\sqrt{(x - 7)^2} = \sqrt{144}$
 $x - 7 = \pm 12$
 $x = 12 + 7$ and $x = -12 + 7$
 $x = 19$ and **$x = -5$**

1) $x^2 - 6x + 9 = 32$

$(x - 3)(x - 3) = 32$
 $(x - 3)^2 = 32$
 $\sqrt{(x - 3)^2} = \sqrt{32}$
 $x - 3 = \pm 4\sqrt{2}$
 $x = \pm 4\sqrt{2} + 3$

$\sqrt{32}$
 $\sqrt{16} \cdot \sqrt{2}$
 $4\sqrt{2}$

2) $4n^2 + 20n + 25 = 2$

$(2n + 5)(2n + 5) = 2$
 $(2n + 5)^2 = 2$
 $\sqrt{(2n + 5)^2} = \sqrt{2}$
 $2n + 5 = \pm \sqrt{2}$
 $2n = \pm \sqrt{2} - 5$
 $n = \frac{\pm \sqrt{2} - 5}{2}$

COMPLETING THE SQUARE

If the equation will not factor into a perfect square, you can "force" it to by inserting the correct number as the third term.

Example: $y^2 + 8y + 11 = 20$
 eleven won't factor, so what number would?
 $y^2 + 8y + \underline{16} = 9 + \underline{16}$
 $(y + 4)(y + 4) = 25$
 $(y + 4)^2 = 25$
 square root both sides
 $\sqrt{(y + 4)^2} = \sqrt{25}$
 $y + 4 = \pm 5$
 $y = 5 - 4$ and $y = -5 - 4$
 $y = 1$ and **$y = -9$**

$\sqrt{-20}$
 $\sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{5}$
 $2i\sqrt{5}$

1) $x^2 - 10x + 45 = 0$

$x^2 - 10x + \underline{25} = -45 + \underline{25}$
 $(x - 5)(x - 5) = -20$
 $(x - 5)^2 = -20$
 $\sqrt{(x - 5)^2} = \sqrt{-20}$
 $x - 5 = \pm 2i\sqrt{5}$
 $x = \pm 2i\sqrt{5} + 5$

2) $3x^2 + 12x + 36 = 0$

Divide everything by 3
 $x^2 + 4x + 12 = 0$
 $x^2 + 4x + \underline{4} = -12 + \underline{4}$
short cut to ()² if you wish
 $(x + 2)^2 = -8$
 $\sqrt{(x + 2)^2} = \sqrt{-8}$
 $x + 2 = \pm 2i\sqrt{2}$
 $x = \pm 2i\sqrt{2} - 2$

3) $-2x^2 + 5x - 3 = 0$

Divide everything by -2
 $x^2 - 5/2x + 3/2 = 0$
 $x^2 - 5/2x + \underline{25/16} = -3/2 + \underline{25/16}$
 $(x - 5/4)^2 = 1/16$
 $\sqrt{(x - 5/4)^2} = \sqrt{1/16}$
 $x - \frac{5}{4} = \pm \frac{1}{4}$
 $x = \pm \frac{1}{4} + \frac{5}{4}$ so $x = 1$ and $x = \frac{3}{2}$