

SOLVING = RATIONAL EQUATIONS

Solve each equation involving addition or subtraction by first finding common denominators,

then.. cross 'em off (forget them)

More examples:

$$2) \quad \frac{y}{y-2} - \frac{3}{2-y} = \frac{2}{5}$$

$$\begin{aligned} 5 \cdot \frac{y}{y-2} - \frac{3 \cdot (-1) \cdot (5)}{2 \cdot (-1) \cdot (5)} &= \frac{2 \cdot (y-2)}{5 \cdot (y-2)} \\ 5y - 3(-1)(5) &= 2(y-2) \\ 5y + 15 &= 2y - 4 \\ 3y &= -19 \\ y &= -19/3 \end{aligned}$$

When in doubt.. factor it out

Oddly, it can get easier... cross multiply

$$1) \quad \frac{9}{28} + \frac{3}{x+2} = \frac{3}{4}$$

$$\begin{aligned} (x+2) \cdot \frac{9}{28} + \frac{3 \cdot 28}{x+2} &= \frac{3 \cdot 7(x+2)}{4 \cdot 7(x+2)} \\ (x+2) \cdot \frac{9}{28} + \frac{84}{x+2} &= \frac{21(x+2)}{28} \\ 9(x+2) + 3(28) &= 21(x+2) \\ 9x + 18 + 84 &= 21x + 42 \\ 9x + 102 &= 21x + 42 \\ 60 &= 12x \\ 5 &= x \end{aligned}$$

$$3) \quad \frac{6}{r+5} + \frac{6}{r-5} = 2$$

$$\begin{aligned} (r-5) \cdot \frac{6}{r+5} + \frac{6 \cdot (r+5)}{r-5} &= \frac{2 \cdot (r+5)(r-5)}{1 \cdot (r+5)(r-5)} \\ (r-5) \cdot \frac{6}{r+5} + \frac{6(r+5)}{r-5} &= \frac{2(r^2 - 25)}{(r+5)(r-5)} \\ 6r - 30 + 6r + 30 &= 2(r^2 - 25) \\ 12r &= 2r^2 - 50 \\ 0 &= 2r^2 - 12r - 50 \quad \text{run program} \\ r &= 8.8, -2.8 \end{aligned}$$

$$4) \quad \frac{2}{x^2-4} - 4 = \frac{1}{3x+6}$$

$$\begin{aligned} 3 \cdot \frac{2}{(x+2)(x-2)} - \frac{4 \cdot 3(x+2)(x-2)}{1} &= \frac{1 \cdot (x-2)}{3(x+2) \cdot (x-2)} \\ \frac{6}{(x+2)(x-2)} - 12(x+2)(x-2) &= \frac{x-2}{3(x+2)(x-2)} \\ 6 - 12(x+2)(x-2) &= x-2 \\ 6 - 12x^2 + 48 &= x-2 \\ 0 &= 12x^2 + x - 56 \quad \text{run program} \\ x &= 2.1, -2.2 \end{aligned}$$

$$5) \quad \frac{w}{w-12} = \frac{4}{7}$$

$$\begin{aligned} w(7) &= 4(w-12) \\ 7w &= 4w - 48 \\ 3w &= -48 \\ w &= -16 \end{aligned}$$

$$6) \quad \frac{2}{x-1} = \frac{x+4}{x-1}$$

$$\begin{aligned} 2(x-1) &= (x+4)(x-1) \\ 2x-2 &= x^2+3x-4 \\ 0 &= x^2+x-2 \\ 0 &= (x+2)(x-1) = 0 \\ x &= -2 \text{ or } x = 1, \text{ but } x \neq 1 \text{ is a} \\ &\quad \text{restriction} \end{aligned}$$

therefore: $x = -2$ only

Can you think of a better way to solve #6?

Restrictions
(excluded or restricted values)

$$7) \quad \frac{1}{d+3} = \frac{2}{d^2-3d-18} - \frac{1}{6-d}$$

$$\begin{aligned} \frac{1}{d+3} &= \frac{2}{d^2-3d-18} - \frac{1}{6-d} \\ \frac{1}{d+3} &= \frac{2}{(d-6)(d+3)} - \frac{1}{-(d-6)} \\ \frac{1}{d+3} &= \frac{2}{(d-6)(d+3)} - \frac{-1}{(d-6)} \\ (d-6) \cdot \frac{1}{d+3} &= \frac{2}{(d-6)(d+3)} + \frac{1}{(d-6)} \cdot (d+3) \\ (d-6) \cdot \frac{1}{d+3} &= \frac{2}{(d-6)(d+3)} + \frac{1 \cdot (d+3)}{(d-6) \cdot (d+3)} \end{aligned}$$

$d-6 = 2+d+3$
 $-6 = 2+3$
 $-6 = 5$ no solution (false statement)

move -1
to the top

Name all restrictions for each equation. You do not need to solve them.

Examples:

$$1) \quad \frac{r}{r-9} = \frac{5}{r+2}$$

$r \neq$ 9, -2

$$2) \quad \frac{1}{3x-2} + x = \frac{8}{x}$$

$x \neq$ 2/3, 0

$$3) \quad \frac{4}{y^2-16} = \frac{y}{2} - \frac{7}{2y^2+3y-20}$$

$(y+4)(y-4)$ $(2y-5)(y+4)$

$y \neq$ 4, -4, 5/2