

Solve the following polynomial equations by factoring or quadratic substitution.

1)  $x^4 - 4x^2 - 12 = 0$

2)  $x^3 + 6x^2 - 4x - 24 = 0$

3)  $3x^3 - 16x^2 - 12x + 64 = 0$

4)  $x^4 - 7x^2 - 8 = 0$

5)  $2x^4 = -7x^2 + 15$

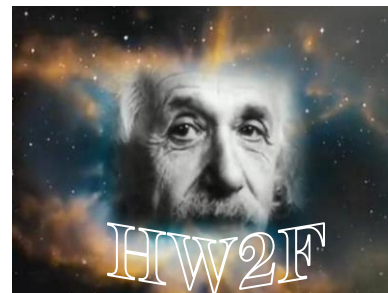
6)  $2x^3 - x^2 - 2x + 1 = 0$

7)  $x^3 + 2x^2 - 6x = 12$

8)  $2x^3 - 3x^2 = 12 - 8x$

9)  $10x^3 + 5x = 6x^2 + 3$

10)  $2x^4 + 3x^2 - 20 = 0$



Create a list of possible rational roots using the rational root theorem (p's & q's). DO NOT SOLVE!

11)  $x^4 - 5x^2 + x - 80 = 0$

12)  $3x^3 - 2x + 5x + 8 = 0$

13)  $10x^5 + 3x^3 + 7x^2 - 2 = 0$

Use the rational root theorem (p's & q's) to solve each equation.

14)  $x^3 - x^2 - x + 1 = 0$

15)  $3x^3 - 4x^2 - 5x + 2 = 0$

16)  $x^4 + 2x^3 - 2x^2 - 6x - 3 = 0$

17)  $3x^4 + 2x^3 - 9x^2 - 12x - 4 = 0$

18)  $2x^4 - x^3 - 7x^2 + x + 2 = 0$

Factor each polynomial function, then use those factors for *sketch* its graph.

19)  $f(x) = x^3 + 2x^2 - 9x - 18$

20)  $g(x) = 4x^3 + x^2 - 18x$

21)  $h(x) = x^4 - 5x^2 + 4$

22)  $k(x) = -x^4 + 10x^2 - 24$

23)  $j(x) = x^4 - 18x^2 + 81$

24)  $f(x) = 4x^3 - 13x - 6$

(hint: you may have to find the first factor using a method other than the one you used for #19-23)

1) $\pm\sqrt{6}, \pm\sqrt{2}$	8) $3/2, \pm 2i$	13) $\pm 1, 2, 1/2, 1/5,$	See Mr. Paull for graphs
2) $-6, \pm 2$	9) $3/5, \pm i\sqrt{2}/2$	$2/5, 1/10$	19) $(x + 3)(x - 3)(x + 2)$
3) $\pm 2, 16/3$	10) $\pm\sqrt{10}/2, \pm 2i$	14) $\pm 1$	20) $x(x - 2)(4x + 9)$
4) $\pm 2\sqrt{2}, \pm i$	11) $\pm 1, 2, 4, 5, 8, 10, 16,$	15) $-1, 1/3, 2$	21) $(x - 1)(x + 1)(x - 2)(x + 2)$
5) $\pm\sqrt{6}/2, \pm i\sqrt{5}$	$20, 40, 80$	16) $-1, \pm\sqrt{3}$	22) $-(x - 2)(x + 2)(x - \sqrt{6})(x + \sqrt{6})$
6) $\pm 1, 1/2$	12) $\pm 1, 2, 4, 8, 1/3, 2/3,$	17) $-1, -2/3, 2$	23) $(x - 3)^2(x + 3)^2$
7) $-2, \pm\sqrt{6}$	$4/3, 8/3$	18) $-1/2, 2, \frac{-1 \pm \sqrt{5}}{2}$	24) $(x - 2)(2x + 1)(2x + 3)$