

The importance of zero....

The senior class has paid \$200 to rent a roller skating rink for a fund-raiser. Tickets for those attending will be \$5



a) Model the net income as a function of the number of tickets sold.

$$n(x) = 5x - 200$$

b) Identify the point at which the class begins to make a profit.

$$\begin{aligned} 5x - 200 &> 0 \\ 5x &> 200 \\ x &> 40 \end{aligned} \quad \text{Every ticket sold after the } 40^{\text{th}} \text{ one is profit.}$$

c) What is their profit if they sell 75 tickets?

$$\begin{aligned} n(x) &= 5x - 200 \\ n(75) &= 5(75) - 200 \\ &= 375 - 200 \\ &= 175 \\ &\text{\$175 profit} \end{aligned}$$

Examples:

1) If $f(x) = \frac{2}{3}x - 12$ find: $f(9)$, $f(-12)$, and the zero of the function

$$\begin{aligned} f(9) &= \frac{2}{3}(9) - 12 \\ &= 6 - 12 \\ &= -6 \end{aligned}$$

$$\begin{aligned} f(-12) &= \frac{2}{3}(-12) - 12 \\ &= -8 - 12 \\ &= -20 \end{aligned}$$

$$\begin{aligned} 0 &= \frac{2}{3}x - 12 \\ 12 &= \frac{2}{3}x \\ 18 &= x \\ \text{the function's zero is } 18 \end{aligned}$$

2) If $g(x) = \frac{3x-11}{2}$ determine if $g(3) + g(5) = g(8)$

$$\begin{aligned} g(3) &= \frac{3(3) - 11}{2} \\ &= \frac{9 - 11}{2} \\ &= \frac{-2}{2} \\ &= -1 \end{aligned}$$

$$\begin{aligned} g(5) &= \frac{3(5) - 11}{2} \\ &= \frac{15 - 11}{2} \\ &= \frac{4}{2} \\ &= 2 \end{aligned}$$

$$\begin{aligned} g(8) &= \frac{3(8) - 11}{2} \\ &= \frac{24 - 11}{2} \\ &= \frac{13}{2} \\ &= 6.5 \end{aligned}$$

$$\begin{aligned} \text{NO.} \\ -1 + 2 &\neq 6.5 \end{aligned}$$

3) If $h(x) = 8$ find: $h(0)$, $h(412)$ and determine the slope of the function

$$\begin{aligned} h(0) &= 8 \\ \text{since there is} \\ \text{nothing to plug in} \\ h(0) &\text{ is literally } 8 \end{aligned}$$

$$\begin{aligned} h(412) &= 8 \\ &= 8 \end{aligned}$$

The function $h(x) = 8$ is called a constant function (there is no variable attached to the 8). Constant functions are horizontal lines so $m = 0$

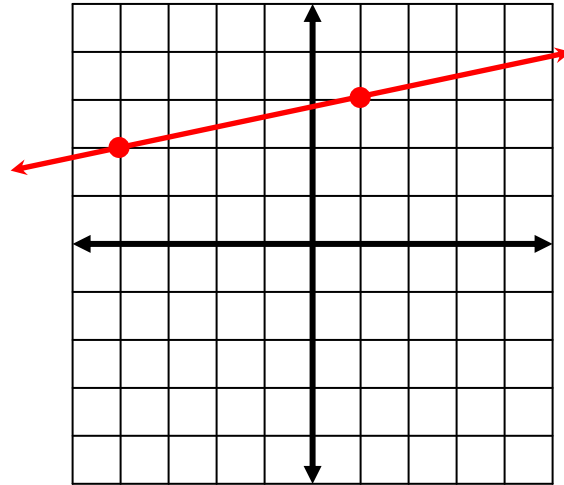
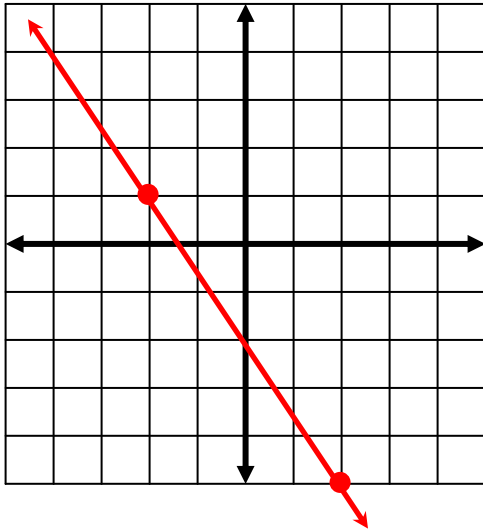
Modeling a linear function by graphing...

Examples: In each of the cases below assume f is a linear function.

Sketch its graph, and find an equation such that...

1) $f(-2) = 1$ and $f(2) = -5$

2) $f(1) = 3$ and $f(-4) = 2$



$m = -3/2$ (count rise over run)
 $y = -3/2x + b$ plug in either pt.
 $1 = -3/2(-2) + b$
 $1 = 3 + b$
 $-2 = b$ $f(x) = -3/2x - 2$

$m = 1/5$
 $y = 1/5x + b$
 $3 = 1/5(1) + b$
 $3 = 1/5 + b$
 $14/5 = b$ $f(x) = 1/5x + 14/5$

Modeling a linear function with data...

Mr. McConnell	Monday	Tuesday	Wednesday	Thursday	Friday
Times seen	4	1	9	6	5
Smart comments	14	5	29	20	17

Write a linear function to represent the number of smart comments Mr. McConnell will deliver as a function of the number of times you see him on any given day.

Treat the data like a set of coordinates,
 pick any two to determine a slope.
 $m = \frac{5-14}{1-4} = \frac{-9}{-3} = 3$
 $y = 3x + b$ pick one of the two you
 $5 = 3(1) + b$ to plug in
 $2 = b$ $M(x) = 3x + 2$