



Sector (of a circle)

SECTORS OF CIRCLES

Formulas:

(if θ is in degrees)

$$s = \frac{\theta}{360} \cdot 2\pi r$$

Area:

$$K = \frac{\theta}{360} \cdot \pi r^2$$

(if θ is in radians)

$$s = r\theta$$

Area:

$$K = \frac{1}{2}r^2\theta \text{ or } K = \frac{1}{2}rs$$

Find the missing measurement. If necessary, round to nearest hundredth.

Examples:

- 1) radius = 5cm
arc length = 8cm
central $\angle = ?$

$$\begin{aligned} 8 &= 5\theta \\ 8/5 &= \theta \\ \theta &= 1.6 \text{ radians} \end{aligned}$$

- 2) radius = 8.2in
central $\angle = 1.52$ radians
arc length = ?

$$\begin{aligned} s &= (8.2)(1.52) \\ s &= 12.464 \text{ in.} \end{aligned}$$

- 3) radius = 10ft
central $\angle = 75^\circ$
arc length = ?

$$\begin{aligned} s &= \frac{75}{360} \cdot 2\pi(10) \\ s &\approx 13.09 \text{ ft.} \end{aligned}$$

- 4) radius = 12mm
central $\angle = 0.44$ radians
area of the sector = ?

$$\begin{aligned} K &= \frac{1}{2}(12)^2(0.44) \\ K &= 31.68 \text{ mm}^2 \end{aligned}$$

- 5) central $\angle = 90^\circ$
radius = 9cm
area of the sector = ?

$$\begin{aligned} K &= \frac{90}{360} \cdot \pi \cdot (9)^2 \\ K &= 63.62 \text{ cm}^2 \end{aligned}$$

- 6) area = 2.178in^2
central $\angle = 0.9$ radians
radius = ?

$$\begin{aligned} 2.178 &= \frac{1}{2}r^2(0.9) \\ 2.178 &= 0.45r^2 \\ 4.84 &= r^2 && \text{square root of 4.84 can't be} \\ r &= 2.2 \text{ in.} && \text{negative (distance)} \end{aligned}$$